Mark Scheme (Results)

January 2016

International Advanced Level
in Core Mathematics C12 (WMA01/01)

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate’s response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate’s response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

1. The total number of marks for the paper is 125.

2. The Edexcel Mathematics mark schemes use the following types of marks:

- **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod – benefit of doubt
- ft – follow through
- the symbol √ will be used for correct ft
- cao – correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw – ignore subsequent working
- awrt – answers which round to
- SC: special case
- oe – or equivalent (and appropriate)
- d… or dep – dependent
- indep – independent
- dp decimal places
- sf significant figures
- ∗ The answer is printed on the paper or ag- answer given
- ⌊ or d… The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the

subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected. If you are using the annotation facility on ePEN, indicate this action by ‘MR’ in the body of the script.

6. If a candidate makes more than one attempt at any question:
   - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
   - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.

8. Marks for each question are scored by clicking in the marking grids that appear below each student response on ePEN. The maximum mark allocation for each question/part question(item) is set out in the marking grid and you should allocate a score of ‘0’ or ‘1’ for each mark, or “trait”, as shown:

	0	1
aM		●
aA	●	
bM1		●
bA1	●	
bB	●	
bM2		●
bA2		●

9. Be careful when scoring a response that is either all correct or all incorrect. It is very easy to click down the ‘0’ column when it was meant to be ‘1’ and all correct.

General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

$(x^2 + bx + c) = (x + p)(x + q)$, where $|pq| = |c|$, leading to $x = \ldots$

$(ax^2 + bx + c) = (mx + p)(nx + q)$, where $|pq| = |c|$ and $|mn| = |a|$, leading to $x = \ldots$

2. Formula

Attempt to use correct formula (with values for *a*, *b* and *c*).

3. Completing the square

Solving $x^2 + bx + c = 0$: $(x \pm \frac{b}{2})^2 \pm q \pm c, \quad q \neq 0$, leading to $x = \ldots$

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. ($x^n \to x^{n-1}$)

2. Integration

Power of at least one term increased by 1. ($x^n \to x^{n+1}$)

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required. Most candidates do show working, but there are occasional awkward cases and if the mark scheme does not cover this, please contact your team leader for advice.

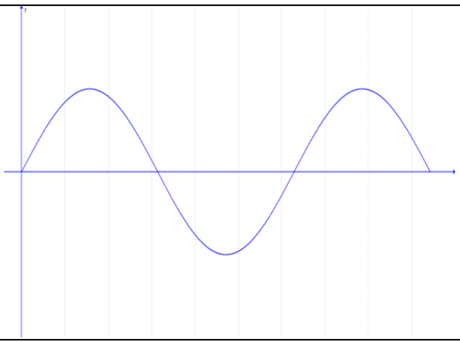
January 2016
Core Mathematics C12
Mark Scheme

Question Number	Scheme	Marks
1(a)	$u_2 = 2\times 2 - 6 = -2, \qquad u_3 = 2\times(-2) - 6 = -10$ or $u_3 = 2\times(2\times 2-6)-6 = -10$	M1 A1
		[2]
(b)	$\sum_{i=1}^{4} u_i = 2 + (-2) + (-10)$	M1
	$+(-26)$	A1ft
	$= -36$	A1
		[3]
		5 marks
	Notes	
(a)	**M1:** Attempt to use the given formula correctly at least once. This may be implied by a correct value for u_2 or a value for u_3 which follows through from their u_2 or implied by correct answer for u_3 **A1**: u_3 correct **and no incorrect work seen**	
(b)	**M1:** Uses sum of the 3 numerical terms from part (a) (may be implied by correct answer for their terms). Attempting to sum an AP here is M0. **A1ft**: obtains u_4 correctly (may be attempted in part (a)) and adds to sum of the first three terms from part (a) **A1**: -36 cao (-36 implies both A marks)	
	Special Cases: Some candidates attempt $u_2 + u_3 + u_4 + u_5$ in part (b) – **allow M1 only** Some candidates mis-copy one of their terms from part (a) into part (b) – **allow M1 only**	

Question Number	Scheme			Marks
2(i)	**Way 1:**	**Way 2:**	**Way 3:**	
	$\frac{49}{\sqrt{7}}=\frac{7^2}{7^{\frac{1}{2}}}=7^{2-\frac{1}{2}}$	$7\sqrt{7}=7^{1+\frac{1}{2}}$	$7^a=\frac{49}{\sqrt{7}}\Rightarrow a=\frac{\log\frac{49}{\sqrt{7}}}{\log 7}$ or $7^a=\frac{49}{\sqrt{7}}\Rightarrow a=\log_7\frac{49}{\sqrt{7}}$	M1
	$(a=)1\frac{1}{2}$ (oe) or see answer $=7^{1\frac{1}{2}}$			A1
				[2]
(ii)	**Way 1:**	**Way 2:**		
	$\frac{10(\sqrt{18}+4)}{(\sqrt{18}-4)(\sqrt{18}+4)}$	$(15\sqrt{2}+20)(\sqrt{18}-4)$		M1
	$=\frac{\cdots}{2}$	$=15\sqrt{36}-60\sqrt{2}+20\sqrt{18}-80$		B1
	$\frac{10}{\sqrt{18}-4}=5\left(3\sqrt{2}+4\right)=15\sqrt{2}+20*$	$=90-60\sqrt{2}+60\sqrt{2}-80$ = 10 so $\frac{10}{\sqrt{18}-4}=15\sqrt{2}+20*$		A1cso
				[3]
				5 marks
	Notes			
(i)	**Way 1:**	**Way 2:**	**Way 3:**	
	M1: Subtracts **their** powers of 7	**M1:** Cancels fraction to $7\sqrt{7}$ and adds **their** powers of 7	**M1:** Correct use of logs to obtain a correct expression for *a*	
	A1: cao (answer only is 2 marks) Do not allow work with inexact decimals for this mark e.g. $49\times7^{-\frac{1}{2}}=18.52\Rightarrow\log18.52=1.4999...\Rightarrow a=1.5$ scores M1A0			
(ii)	**Way 1:**	**Way 2:**		
	M1: Multiply numerator and denominator by $\sqrt{18}+4$ or equivalent. The statement $\frac{10(\sqrt{18}+4)}{(\sqrt{18}-4)(\sqrt{18}+4)}$ is sufficient but do not allow $\frac{10(\sqrt{18}+4)}{\sqrt{18}-4(\sqrt{18}+4)}$ unless missing brackets are implied by subsequent work. **B1:** Correctly obtains ±2 in the denominator (**Must follow M1 – i.e. treat as A1**). May be implied by e.g. $\frac{10(\sqrt{18}+4)}{18-16}=5\left(\sqrt{18}+4\right)$ **A1**: Correct result with no errors seen and $\sqrt{18}=3\sqrt{2}$ **used before their final answer.** Note that for **Way 1**, correct work leading to $5\sqrt{18}+20$ followed by $15\sqrt{2}+20$ with no intermediate step would lose the final mark	**M1:** Attempts to expand $(15\sqrt{2}+20)(\sqrt{18}-4)$ to obtain at least 3 (not necessarily correct) terms **B1:** All 4 terms correct (**Must follow M1 – i.e. treat as A1**) **A1**: Obtains 10 with no errors and $\sqrt{18}=3\sqrt{2}$ seen or implied by e.g. $20\sqrt{18}=60\sqrt{2}$ **and** conclusion that states the given answer i.e. not just 10 = 10		

Question Number	Scheme	Marks
3.	$\int\left(6x-3-\frac{2}{\sqrt{x}}\right)\mathrm{d}x=\frac{6x^2}{2}-3x-\frac{2x^{\frac{1}{2}}}{\frac{1}{2}}+(c)$	M1 A1 A1
	$\left[\frac{6x^2}{2}-3x-\frac{2x^{\frac{1}{2}}}{\frac{1}{2}}+(c)\right]_1^4=(28)-(-4)=32$	M1 A1
		[5]
		5 marks
	Notes	
	M1: Attempt to integrate original f(x) – at least one power increased $x^n \to x^{n+1}$ **A1: Two** of the three terms **correct un-simplified or simplified** (**Constant not required**) **A1:** All three terms **correct un-simplified or simplified** (**Constant not required**) **M1:** Substitutes limits 4 and 1 into their 'changed' function and subtracts the right way round **A1:** 32 cao **(32 + c is A0)** **The question requires the use of calculus so a correct answer only scores no marks)**	

Question Number	Scheme	Marks
4.	$a+3d=3$ **OR** $\frac{6}{2}(2a+5d)=27$	M1 A1
	$a+3d=3$ **AND** $\frac{6}{2}(2a+5d)=27$	A1
	Eliminates one variable to find a or d from 2 equations in a and d	dM1
	Obtains $a = 12$ **or** $d = -3$	A1
	Obtains $a = 12$ **and** $d = -3$	A1
		[6]
		6 marks
	Notes	
	M1A1: Writes down a correct (possibly un-simplified) equation for 4th term **or** for sum of the first 6 terms. Allow the individual terms to be added for the sum e.g. $a+a+d+a+2d+a+3d+a+4d+a+5d=27$ **A1cao:** A correct equation for 4th term **and** a correct equation for the sum (allow either to be un-simplified) **dM1:** Eliminates one variable from two equations in a and d to find either a or d (see note below) **A1:** One variable correct (This implies previous M mark) **A1:** Both variables correct Note that if both equations are correct and there is **no working** and the values of a and d are both incorrect, this scores dM0. Also if either or both equations is/are incorrect and values of a and d are obtained with **no working** this also scores dM0.	

<table>
<tr><th>Question number</th><th colspan="2">Scheme</th><th>Marks</th></tr>
<tr><td rowspan="3">5(a)</td><td rowspan="2"></td><td>Sketch of a positive sine curve- passing through O with at least one complete cycle from O. Condone different amplitudes above and below the x-axis.</td><td>B1</td></tr>
<tr><td>Correct shape with one and a half cycles as shown (from O to $\frac{3\pi}{2}$) and crossing the x–axis at $\frac{\pi}{2}$ and π</td><td>B1</td></tr>
<tr><td colspan="2"></td><td>[2]</td></tr>
<tr><td rowspan="5">(b)</td><td colspan="2">
<table>
<tr><td>x</td><td>0</td><td>$\frac{\pi}{12}$</td><td>$\frac{\pi}{6}$</td><td>$\frac{\pi}{4}$</td></tr>
<tr><td>y</td><td>0</td><td>0.5</td><td>0.866</td><td>1</td></tr>
</table>
</td><td></td></tr>
<tr><td colspan="2">Uses $\frac{1}{2}\times\frac{\pi}{12}$
May be implied by use of e.g. $\frac{1}{2}h=\frac{1}{2}\left(\frac{\pi}{6}-\frac{\pi}{12}\right)=\frac{1}{2}(0.261....)$</td><td>B1</td></tr>
<tr><td colspan="2">$....\{(0+1)+2(0.5+0.866)\}$</td><td>M1</td></tr>
<tr><td colspan="2">0.4885176576… awrt 0.49</td><td>A1</td></tr>
<tr><td colspan="2"></td><td>[3]</td></tr>
<tr><td></td><td colspan="2"></td><td>5 marks</td></tr>
<tr><td></td><td colspan="3">Notes</td></tr>
<tr><td>(a)</td><td colspan="3">Notes as above
B1: Correct shape with positive gradient through O
B1: Need not see endpoints labelled. Ignore any part of the curve to the left of the origin but if the curve extends beyond $x=\frac{3\pi}{2}$ then then $x=\frac{3\pi}{2}$ must be labelled on the diagram. Labels for $\frac{\pi}{2}$ and π may be on the diagram or in the text but not just in a table of values and must be in radians not degrees. (Allow awrt 1.57 and 3.14)
The amplitudes must not be significantly different above and below the x-axis.</td></tr>
<tr><td>(b)</td><td colspan="3">B1: Need ½ of $\frac{\pi}{12}$ or to see $\frac{\pi}{24}$ or ½ of 0.261….
M1: requires first bracket to contain first plus last values and second bracket to include no additional values from the two in the table.
If values used in brackets are x values instead of y values this scores M0.
A1: for awrt 0.49
Separate trapezia may be used: B1 for $\frac{\pi}{24}$ and M1 for ½$h(a+b)$ used 3 times
Special Case: Bracketing mistake: i.e. $\frac{\pi}{24}(0+1)+2(0.5+0.866)\ (=2.86...)$
scores B1 M1 A0 unless the final answer implies that the calculation has been done correctly (then full marks can be given).
Need to see trapezium rule used so answer only (with no working) is 0/3</td></tr>
</table>

Question Number	Scheme	Marks
6.	$\text{f}(x) = x^3 + x^2 - 12x - 18$	
(a)	Attempts $\text{f}(\pm 3)$	M1
	$\{\text{f}(-3)=\}$ 0 so $(x + 3)$ is a factor of $\text{f}(x)$.	A1
		[2]
(b)	$x^3 + x^2 - 12x - 18 = (x+3)(x^2 + ...$	M1
	$x^3 + x^2 - 12x - 18 = (x+3)(x^2 - 2x - 6)$ or $x^3 + x^2 - 12x - 18 = (x+3)(x-1+\sqrt{7})(x-1-\sqrt{7})$ oe	A1
		[2]
(c)	$(x =)\ -3$	B1
	$x = \dfrac{2 \pm \sqrt{4+24}}{2} = 1 \pm \sqrt{7}$ or by completion of square $(x-1)^2 = 7$ so $x = 1 \pm \sqrt{7}$ or $\left(x-1+\sqrt{7}\right)\left(x-1-\sqrt{7}\right) = 0 \Rightarrow x = 1 \pm \sqrt{7}$	M1 A1
		[3]
		7 marks
	Notes	
(a)	**M1**: As on scheme – must use the factor theorem **A1:** for seeing 0 and conclusion which may be in a preamble and may be minimal e.g. QED, proven, true, tick etc. There must be no obvious errors but need to see at least $(-3)^3 + (-3)^2 - 12(-3) - 18 = 0$ for A1 but allow invisible brackets e.g. $-3^3 + -3^2 - 12(-3) - 18 = 0$ provided there are no obvious errors.	
(b)	**M1**: Uses $(x + 3)$ as a factor and obtains correct first term of quadratic factor by division or any other method e.g. comparing coefficients or finding roots and factorising **A1 :** Correct quadratic and writes $(x+3)(x^2 - 2x - 6)$ or $(x+3)(x-1+\sqrt{7})(x-1-\sqrt{7})$ oe Note that this work may be done in part (a) and the result re-stated here.	
(c)	**B1:** States -3 **M1:** Method for finding their roots. Allow the usual rules applied to their quadratic. **This mark is for finding the roots and not for just finding factors. You may need to check their roots if no working is shown e.g. if they give decimal answers (3.645…, -1.645…)** **A1:** need both roots. Correct answer implies M mark. Allow $x = \dfrac{2 \pm \sqrt{28}}{2}$ If they give extra roots e.g. $x = -3,\ -1,\ \dfrac{2 \pm \sqrt{28}}{2}$, lose the final A mark (B1M1A0)	

Question Number	Scheme	Marks
7(a)	$\left(1+kx\right)^8=1+\binom{8}{1}(kx)+\binom{8}{2}(kx)^2+\binom{8}{3}(kx)^3\ldots$	M1
	$=1+8kx,+28k^2x^2,+56k^3x^3+\ldots$	B1, A1, A1
		[4]
(b)	Sets $"56k^3"=1512$ and obtains $k^3=\dfrac{1512}{56}$	M1 A1
	So $k=3$	A1
		[3]
		7 marks
	Notes	
(a)	**M1**: The **method** mark is awarded for an attempt at the Binomial expansion to get the third **and/or** fourth term. The **correct** binomial coefficient needs to be combined with the correct power of *x*. Ignore bracket errors and omission of or incorrect powers of *k*. Accept any notation for ${}^8C_2$ or ${}^8C_3$, e.g. $\binom{8}{2}$ or $\binom{8}{3}$ or 28 or 56 from Pascal's triangle. This mark may be given if no working is shown, but either or both of $28k^2x^2$ and $56k^3x^3$ is found. **B1:** This is for 1 + 8*kx* and not for just $1+\binom{8}{1}(kx)$ **A1:** is cao and is for $28k^2x^2$ or for $28(kx)^2$ **A1:** is cao and is for $56k^3x^3$ or for $56(kx)^3$ Any extra terms in higher powers of *x* should be ignored. Allow terms separated by commas or given as a list for all the marks.	
(b)	**M1:** Sets their coefficient of $x^3=1512$ and obtains $k^n=..$ where *n* is 1 or 3 **A1:** $k^3=\dfrac{1512}{56}$ or equivalent e.g. 27 (May be implied by their final answer) **A1:** *k* = 3 cao (±3 is A0) **Note (b) can be marked independently of part (a) so part (a) might be incorrect or not attempted but they have $56k^3=1512$ etc. in (b)**	

Question Number	Scheme	Marks
	$7\sin x = 3\cos x$	
8(a)	$(\tan x =)\dfrac{3}{7}$	B1
		[1]
(b)	$\tan(2\theta + 30) = \dfrac{3}{7}$	B1ft
	$\tan^{-1}"\dfrac{3}{7}"\ (\alpha)$	M1
	One of $\theta =$ awrt 87 or awrt 177 or awrt 267 or awrt 357	A1
	Follow through any of their final θ's for $\theta \pm 90n$ within range	A1ft
	All of $\theta =$ 86.6, 176.6, 266.6, 356.6	A1
		[5]
		6 marks
	Notes	
(a)	**B1: (** $\tan x =)\dfrac{3}{7}$ or exact equivalent so accept recurring decimal ($0.428571...$) but not rounded answer	
(b)	**B1ft:** Correct equation as shown or follow through their value for tan x from part (a). Must be $\tan(2\theta+30) = \ldots$ but $2\theta + 30$ may be implied later by an attempt to subtract 30 and then divide by 2. If the processing is unclear or incorrect and $2\theta + 30$ is never seen, score B0 here. **M1:** Finds arctan of their $\dfrac{3}{7}$. Could be implied by their value e.g. 23.19.. or just $\tan^{-1}"\dfrac{3}{7}"$ **A1:** For **one** of either $\theta =$ awrt 87 or awrt 177 or awrt 267 or awrt 357 **A1ft:** Follow through any of their **final** answers to which an integer multiple of 90 has been added or subtracted to give another solution in range **but not for adding a multiple of 90 to just α.** **A1: For all 4 correct answers to the required accuracy as stated in the scheme**. Ignore extra answers outside range but lose last A mark for extra answers inside range.	

Question Number	Scheme	Marks
9.(a)	$130000\times(1.02)=132600*$ or $2\%=2600$ and $130000+2600=132600*$	B1
		[1]
(b)	$(r=)\ 1.02$	B1
		[1]
(c)	Uses $130000\times(1.02)^{N-1}>260000$ **or** $130000\times(1.02)^{N-1}=260000$	M1
	So $(1.02)^{N-1}>2$	A1
	$(N-1)\log_{10}(1.02)>\log_{10}2$ or $(N-1)\log_{10}(1.02)=\log_{10}2$ or $(N-1)>\log_{1.02}2$ or $(N-1)=\log_{1.02}2$	M1
	$N>\dfrac{\log_{10}2}{\log_{10}(1.02)}+1*$	A1cso
		[4]
(d)	$(N=)\ 37$	B1
		[1]
		7 marks
	Notes	
(a)	**B1:** A reason must be provided for this mark as the answer is printed. **Allow both** $130000\times(1+2\%)$ **and** $130000\times(102\%)$ **as both give the correct answer when entered this way on a calculator. But not** $130000\times1+2\%$	
(b)	**B1:** For 1.02 oe e.g. allow $\dfrac{51}{50}$	
(c)	**M1: Correct** inequality or equality – may use *r* or their *r* or 1.02 and may use *N* or *n*. **A1:** $(1.02)^{N-1}>2$ cao. Allow $(1.02)^{n-1}>2$ **M1:** Correct use of logs power rule on their previous line which must have come from using the n^{th} term of a GP. Condone missing brackets for this mark e.g. $N-1\log_{10}(1.02)>\log_{10}2$. (May follow use of $=$ instead of $>$ or use of *r* instead of 1.02 or use of *N* instead of *N* - 1). These cases can get M0A0M1. Allow the base to be absent or just 'ln' for this mark. If the inequality sign is reversed at this point, still allow the M1. **A1*:** Answer is **exactly** as printed (**including the bases**) and **all** inequality work should be correct and all previous marks scored and **no missing brackets earlier.** Allow this mark to score from a correct previous line provided the power rule is used. So fully correct work leading to $(N-1)\log_{10}(1.02)>\log_{10}2\Rightarrow N>\dfrac{\log_{10}2}{\log_{10}(1.02)}+1$ **scores the final M1A1 but** $(1.02)^{N-1}>2\Rightarrow N>\dfrac{\log_{10}2}{\log_{10}(1.02)}+1$ **scores M0A0 (no explicit use of power rule)**	
(d)	**B1:** Only need $N=37$ – may follow trial and error or uses logs to a different base. Do not allow $N\geq37$ or $N>37$ or $N=37.0$	

Question Number	Scheme	Marks
	$y = 12x^{\frac{5}{4}} - \frac{5}{18}x^2 - 1000$	
10.(a)	$\frac{dy}{dx} = 12 \times \frac{5}{4}x^{\frac{1}{4}} - \frac{10}{18}x$	M1 A1
		[2]
(b)	Put $12 \times \frac{5}{4}x^{\frac{1}{4}} - \frac{10}{18}x = 0$ so $x^n = k \quad (n \in \square,\ k \neq 0)$	M1
	$\therefore\ x = (\ )^{\frac{4}{3}}$	dM1
	$\therefore\ x = 81$ **(Ignore *x* = 0 if given as a second solution)**	A1
	So $y = 12(81)^{\frac{5}{4}} - \frac{5}{18}(81)^2 - 1000$ i.e. $y = 93.5$	dM1A1
		[5]
(c)	$\frac{d^2y}{dx^2} = = \frac{15}{4}x^{-\frac{3}{4}} - \frac{5}{9}$	B1ft
	Substitutes their non-zero *x* (positive or negative) into their second derivative.	M1
	Obtains maximum after correctly substituting 81 into correct second derivative to give correct negative quantity $-\frac{15}{36}$ o.e. or decimal e.g. -0.4…. (see note below) and considers negative sign deducing maximum. Note that a correct second derivative followed by $x = 81 \Rightarrow \frac{d^2y}{dx^2} = \frac{15}{4}81^{-\frac{3}{4}} - \frac{5}{9} = -\frac{5}{12}$ therefore maximum scores B1M1A0 here.	A1
		[3]
		10 marks
	Notes	
(a)	**M1:** Attempt to differentiate – power reduced by one $x^n \to x^{n-1}$ (but not just 1000 $\to$ 0) **A1:** Two correct terms and no extra terms. Terms may be un-simplified.	
(b)	**M1:** Puts derivative = 0 and attempts to solve to obtain an equation of the form $x^n = k$ where *n* is real and *k* is non-zero **dM1:** Correct processing to obtain a value for *x*. (Dependent on the first method mark). This mark can only be awarded for processing an equation of the form $ax^{\frac{1}{4}} - bx = 0$ i.e. their derivative must have the **correct powers of *x*.** E.g. $ax^{\frac{1}{4}} - bx = 0 \Rightarrow x^{\frac{1}{4}}\left(a - bx^{\frac{3}{4}}\right) \Rightarrow x = k^{\frac{4}{3}}$ or $ax^{\frac{1}{4}} - bx = 0 \Rightarrow ax^{\frac{1}{4}} = bx \Rightarrow px = qx^4 \Rightarrow x = \sqrt[3]{k}$ Do not allow incorrect squaring e.g. $ax^{\frac{1}{4}} - bx = 0 \Rightarrow px - qx^4 = 0$ etc. **A1:** cao **dM1:** Substitutes their **positive** value for *x* into *y* = … **and not into** $\frac{dy}{dx} = \ldots$ (Dependent on the first method mark) **A1:** cao If *x* = 81 appears from **no working** following a correct derivative score M1M0A0 then allow full recovery.	
(c)	**B1ft:** Correct **follow through** second derivative **M1:** Substitutes their non-zero *x* (**positive or negative**) into their second derivative. **Note**: Solving $\frac{d^2y}{dx^2} = 0$ is M0 **A1cso:** Completely correct work ($-\frac{5}{12}$ o.e.) . Note that o.e. could be $= \frac{15}{4} \times \frac{1}{27} - \frac{5}{9}$ or $\frac{15}{108} - \frac{5}{9}$ or $\frac{5}{36} - \frac{5}{9}$ or -0.4….**but it has to be correct for the final mark.**	

Question Number	Scheme	Marks
11(a)	$16^2 = 10^2 + 12^2 - 2\times10\times12\cos\angle YXZ$	M1
	$\cos\angle YXZ = \dfrac{10^2+12^2-16^2}{2\times10\times12}$ or $\dfrac{-12}{240}$ or -0.05	A1
	$\angle BOC = 1.62(08..)$ (N.B. 92.87 degrees is A0)	A1
		[3]
(b)	Uses $s = 5\theta$ with their θ from part (a)	M1
	awrt 8.1	A1
	Perimeter $= r\theta + 28,\ = 28 +$ their arc length	M1
	awrt 36.1	A1
		[4]
(c)	area of sector $= \tfrac{1}{2}(5)^2\theta$	B1ft
	area of triangle $= \tfrac{1}{2}10\times12\sin\theta$ ($= 59.92$ *or* 59.93)	B1ft
	Area of shaded region $= \tfrac{1}{2}\times10\times12\sin\theta - \tfrac{1}{2}(5)^2\theta$ = 59.9… - 20.2… = 39.7 (cm^2)	M1 A1
		[4]
		(11 marks)
	Notes	
(a)	**M1:** Uses cosine rule – must be a correct statement **A1:** Correct value or correct numerical expression for $\cos\angle YXZ$ **A1:** accept awrt 1.62 and must be seen in part (a) (answer in degrees is A0 (92.865…))	
(b)	**M1:** Uses $s = 5\theta$ with their θ in radians, or correct formula for degrees if working in degrees **A1:** Accept awrt 8.1 (may be implied by their perimeter) **M1:** Adds their arc length to 28 or (16 + 7 + 5) **A1:** Accept awrt 36.1 do not need units (ignore any given)	
(c)	**B1ft:** This formula **used** with their θ in radians or correct formula for degrees **B1ft:** Correct formula for area **used** – may use half base times height (may be implied by a correct answer (59.9…)) **M1:** Subtracts their sector area from their triangle area **this way round**. **A1:** awrt 39.7 – do not need units (ignore any given)	
	<u>Alternative approach to finding angle YXZ and area of triangle:</u> Let foot of perpendicular from X to YZ be W and $XW = h$ and $YW = x$ so $WZ = 16 - x$: $h^2 + x^2 = 100,\quad h^2 + (16-x)^2 = 144 \Rightarrow x = \dfrac{53}{8}, h = \dfrac{3\sqrt{399}}{8}$ M1: Correct work leading to values of x and h $\angle YXZ = \sin^{-1}\left(\dfrac{53}{80}\right) + \sin^{-1}\left(\dfrac{25}{32}\right) = 1.62$ A1: Correct expression for $\angle YXZ$, A1: awrt 1.62 The B1 for the triangle area in (c) can then score for $\dfrac{1}{2}\times16\times"\dfrac{3\sqrt{399}}{8}"$. Note this is $3\sqrt{399}$	

Question Number	Scheme	Marks
	(a) and (b) can be marked together	
12(a)	$\mathrm{f}(x)=\dfrac{16+24\sqrt{x}+9x}{x}$	M1
	$\mathrm{f}(x)=16x^{-1}+24x^{-\frac{1}{2}}+9$	M1A1A1
		[4]
(b)	$\mathrm{f}'(x)=-16x^{-2}-12x^{-\frac{3}{2}}$	M1 A1
		[2]
(c)	When $x = 4$, $y = 25$	B1
	$\mathrm{f}'(4)=-1-\dfrac{12}{8}=-2\tfrac{1}{2}$	M1
	Equation of tangent is $y-25=-\dfrac{5}{2}(x-4)$	M1 A1
		[4]
		10 marks
	Notes	
(a)	**M1:** expands numerator into a three (or four) term quadratic in √x (allow $\left(\sqrt{x}\right)^2$ for x) **M1:** Divides at least one term in numerator by x correctly following an attempt at expansion. May just be $\dfrac{16}{x}$. **A1:** Two correct terms **A1:** All terms correct	
(b)	**M1:** Evidence of differentiation $x^n \to x^{n-1}$ of an expression of the form Ax^{-1} **or** Bx^k so $x^{-1}\to x^{-2}$ **or** $x^k \to x^{k-1}$ $(k \neq 1)$ and not just $C \to 0$. Differentiating top and bottom separately is M0. Note this is a hence and so attempts at e.g. use of the quotient rule scores M0. **A1:** cao and cso (May be un-simplified) **Note: An incorrect constant in part (a) (e.g. 3 instead of 9) will fortuitously give the same derivative so scores M1A0 if otherwise correct.**	
(c)	**B1:** 25 only **M1:** Substitute $x = 4$ into their derived function **M1:** Uses their "25" and their "gradient" which has come from calculus (**not the normal gradient**) and $x = 4$ to give correct ft equation of line. If using $y = mx + c$ must at least obtain a value for c **A1:** any correct form e.g. $y=-\dfrac{5}{2}x+35, \quad 5x+2y-70=0$ **BUT NOT JUST** $\dfrac{y-25}{x-4}=-\dfrac{5}{2}$**, this scores M1A0** **Note: An incorrect constant in part (a) (e.g. 3 instead of 9) will fortuitously give the correct answer in (c) and will lose the final A mark if otherwise correct.**	

Question Number	Scheme	Marks
13(a)	$3kx^2+(8k+6)x+9k-2=0$ or $3kx^2+8kx+6x+9k-2=0$	B1
	Uses b^2-4ac with $a=3k, b=8k\pm 6$ and $c=9k\pm 2$	M1
	$-44k^2+120k+36<0$ or $36<44k^2-120k$ o.e. **Reached with no errors**	A1
	$11k^2-30k-9>0$ *	A1*
		[4]
(b)	Attempts to solve $11k^2-30k-9=0$ to give $k=$	M1
	$\Rightarrow$ Critical values, $k=3, -\frac{3}{11}$	A1
	$k>3$(or) $k<-\frac{3}{11}$	M1 A1cao
		[4]
		8 marks
	Notes	
(a)	**B1:** Multiplies by k and collects terms to one side in any order. Allow the x terms not to be combined and the '= 0' may be implied by use of a **correct** discriminant. **M1:** Attempts b^2-4ac with $a=3k, b=8k\pm 6$ and $c=9k\pm 2$ or uses quadratic formula with b^2-4ac seen to solve their equation or uses $b^2=4ac$ or e.g. $b^2<4ac$. **There must be no *x*'s.** **A1: Obtains a correct three term quadratic inequality** that is not the printed answer with **no errors seen.** **A1:** Correct answer with **no errors**	
(b)	**M1:** Uses factorisation, formula, or completion of square method to find **two values** for k or finds two **correct** answers with no obvious method for **<u>the given</u>** three term quadratic **A1:** Obtains $k=3, -\frac{3}{11}$ accept awrt - 0.272 **M1: Chooses outside region (**$k<$ Their Lower Limit $k>$ Their Upper Limit) for a 3 term quadratic inequality. Do not award simply for diagram or table. **A1:** $k>3$(or) $k<-\frac{3}{11}$ must be exact here but allow $-0.\dot{2}\dot{7}$ for $-\frac{3}{11}$. Allow other notation such as $\left(-\infty,-\frac{3}{11}\right)\cup(3,\infty)$ $k>3$ **and** $k<-\frac{3}{11}$ and $-\frac{3}{11}>k>3$ score M1A0 ISW if possible e.g. $k>3$, $k<-\frac{3}{11}$ followed by $-\frac{3}{11}>k>3$ can score M1A1 $k>3$, $k>-\frac{3}{11}$ followed by $k>3$(or) $k<-\frac{3}{11}$ can score M1A1 Allow (b) to be solved in terms of x for the first 3 marks but the final A mark needs the regions in terms of k. **Fully correct answer with no working scores full marks.** **Answers that are otherwise correct but use $\leq, \geq$ lose final mark.**	

Question Number	Scheme	Marks
14(i)	$\log_a x+\log_a 3=\log_a 27-1$ so $\log_a \frac{3x}{27}=-1$ Or $\log_a x+\log_a 3=\log_a 27-\log_a a$ so $\log_a 3x=\log_a \frac{27}{a}$ Or $\log_a x+1=\log_a 27-\log_a 3=\log_a 9$ so $\log_a ax=\log_a 9$	M1 A1
	$\frac{3x}{27}=a^{-1}$	M1
	$x=9a^{-1}$ or $\frac{9}{a}$	A1
		[4]
(ii)	$x^2-7x+12=0$ and attempt to solve to give $x=\dots$ or $\log_5 y=\dots$ (implied by correct answers)	M1
	x (or $\log_5 y$) = 3 **and** 4	A1
	$y=5^3$ **or** 5^4	dM1
	y = 125 **and** 625	A1
		[4]
		8 marks
	Notes	
(i)	**M1**: Uses sum or difference of logs correctly e.g. $\log x+\log 3=\log 3x$ or $\log 27-\log 3=\log 9$ or $\log 27-\log x=\log\frac{27}{x}$ etc. or writes 1 as $\log_a a$ **A1:** Uses **two** rules correctly to obtain correct log equation **M1:** Removes logs correctly to obtain an equation connecting x and a **A1:** Correct simplified answer Note that some candidates interpret $\log_a 27-1$ as $\log_a(27-1)$. This can score a maximum of 1 out of 4 if they have $\log x+\log 3=\log 3x$ Note that $\log_a x+\log_a 3=\log_a 27-1$ so $\frac{\log_a 3x}{\log_a 27}=-1\Rightarrow\frac{3x}{27}=a^{-1}$ etc. scores **M1A0M0A0** Note that $\log_a x+\log_a 3=\log_a 27-1$ so $\frac{\log_a x\log_a 3}{\log_a 27}=-1\Rightarrow\frac{3x}{27}=a^{-1}$ etc. scores **no marks**	
(ii)	**M1:** Recognise and attempt to solve quadratic **A1:** Obtain both 3 and 4 (Both correct implies M1A1) **dM1:** Uses powers **correctly** to find a value for y **(Dependent on first method mark)** **A1:** Both values correct	

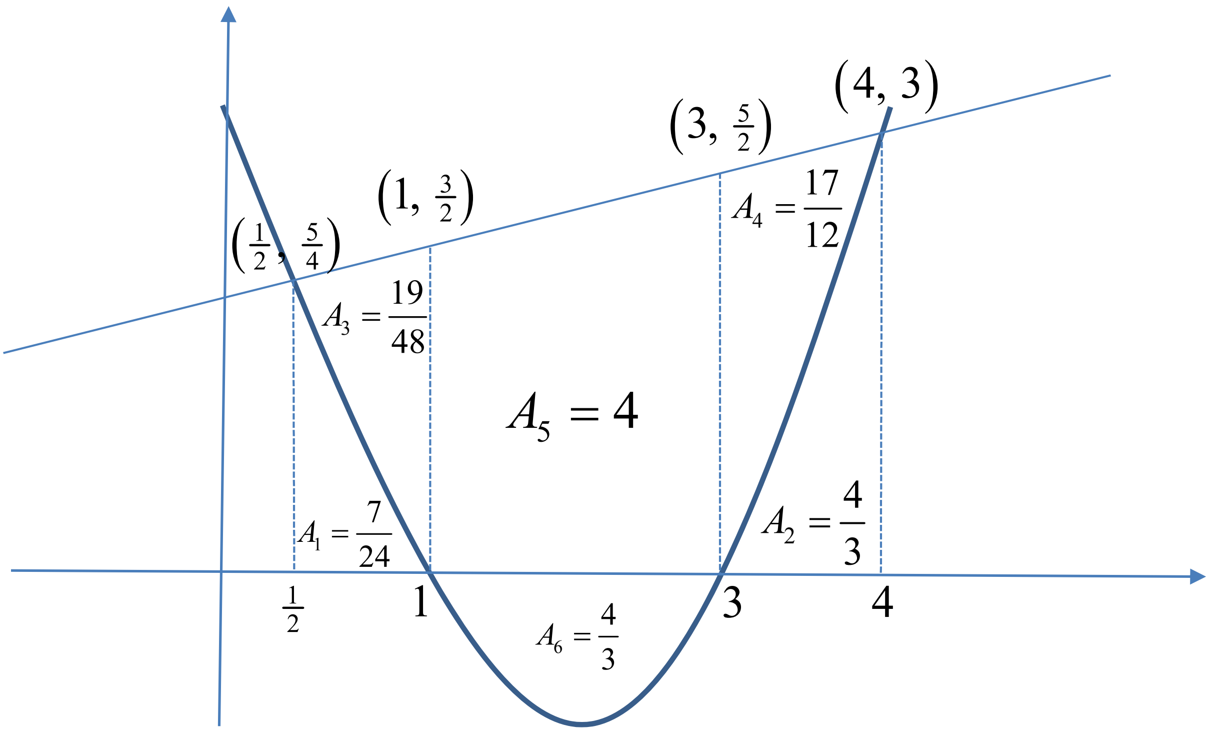
Question Number	Scheme	Marks
15 (a)	Mid-point of AB = (2, - 3)	M1 A1
	$(r^2) = (12 - "2")^2 + (2 - "-3")^2$ or $(r^2) = (-8 - "2")^2 + (-8 - "-3")^2$ or $(d^2) = (-8 - 12)^2 + (-8 - 2)^2$	M1
	$r^2 = 125$	A1
	$"125" = (\boldsymbol{x} \pm "2")^2 + (\boldsymbol{y} \pm "-3")^2$	M1
	$125 = (x-2)^2 + (y+3)^2$	A1
		[6]
(b)	gradient from "(2, −3)" to (4, 8) $= \dfrac{8 - "-3"}{4 - "2"}, \left(= \dfrac{11}{2}\right)$	M1
	ZM has gradient $-\dfrac{1}{m}$ $\left(= -\dfrac{2}{11}\right)$	M1
	Either : $y - 8 = "-\tfrac{2}{11}"(x-4)$ **or**: $y = "-\tfrac{2}{11}"x + c$ and $8 = "-\tfrac{2}{11}"(4) + c \Rightarrow c = "8\tfrac{8}{11}"$	ddM1
	$2x + 11y - 96 = 0$	A1
		[4]
		(10marks)
	Notes	
(a)	**M1:** Uses midpoint formula, or implied by y coordinate of -3 or x coordinate of 2 **A1:** cao **M1:** Finds radius or radius^2, diameter or diameter^2 using any valid method – probably distance from centre to one of the points. **Need not state *r* =… so ignore lhs – you are just looking for correct use of Pythagoras with or without the square root so ignore how they reference it for this mark.** **A1:** for any equivalent $r^2 = 125$ or $r = \sqrt{125}$ (11.18...) etc . Their numeric answer must be identified here as either r or r^2 (may be implied by their equation). If they halve it or double it, this is M1 A0. **M1:** Attempt to use a true equation for circle with their centre and radius or the letter r, allow sign slips in brackets but do not allow use or r instead of r^2 in the equation. So must be using $r^2 = (\boldsymbol{x} \pm ...)^2 + (\boldsymbol{y} \pm ...)^2$ **A1:** correct answer only (Allow $\left(5\sqrt{5}\right)^2$ instead of 125 but not $5\sqrt{5}\,^2$)	
(b)	**M1:** States or uses gradient equation correctly **with their centre and (4, 8).** Must be using their centre and (4, 8). If no method is shown and gradient incorrect for their values score M0. **M1:** Finds negative reciprocal. Follow through their gradient **ddM1:** Correct straight line method with (4, 8) and perpendicular gradient. Dependent on **both** previous method marks having been scored. **A1:** cao – accept multiples of this equation **(Note integer coefficients not required)** A common error here is to use the diameter to find the gradient. This usually scores M0M1ddM0A0 i.e. just one mark for the perpendicular gradient rule.	
	(b) Alternative uses implicit differentiation: e.g. $125 = (x-2)^2 + (y+3)^2 \Rightarrow 2(x-2) + 2(y+3)\dfrac{\mathrm{d}y}{\mathrm{d}x} = 0$ M1(correct implicit differentiation) oe $\Rightarrow \dfrac{\mathrm{d}y}{\mathrm{d}x} = \dfrac{2-x}{y+3} = \dfrac{2-4}{8+3}$ M1(Substitution) Then follow the scheme.	

Question Number	Scheme	Marks
16(a)	$\frac{1}{2}x+1=x^2-4x+3$	M1
	$2x^2-9x+4=0 \Rightarrow$ x = ½ or x = 4	dM1 A1
	y = 5/4 or y = 3	dM1 A1
		[5]
(b)	Curve meets x-axis at $x=3$ and at x = 1 **(No need to see y = 0)**	M1 A1
		[2]
	NOTE that the subscripted A's refer to areas on the diagram given at the end of the scheme. **All the method marks are for <u>their</u> x = 1/2 , 4, 1 and 3**	
(c) **Way 1**	$\int x^2-4x+3\,\mathrm{d}x=\frac{1}{3}x^3-2x^2+3x$	M1 A1
	Use limits 1 and ½ $[(\frac{1}{3}(1)^3-2(1)^2+3\times 1)-(\frac{1}{3}(\frac{1}{2})^3-2.(\frac{1}{2})^2+3\times(\frac{1}{2}))]$ A_1	M1
	Use limits 4 and 3 $[(\frac{1}{3}(4)^3-2(4)^2+3\times(4))-(\frac{1}{3}(3)^3-2.(3)^2+3\times(3))]$ A_2	M1
	Area of trapezium = $\frac{1}{2}(a+b)\times h=\frac{1}{2}(\frac{5}{4}+3)\times(4-\frac{1}{2})=...$ or $\int_{\frac{1}{2}}^{4}(\frac{1}{2}x+1)\mathrm{d}x=\left[\frac{1}{4}x^2+x\right]_{\frac{1}{2}}^{4}=(4+4)-(\frac{1}{16}+\frac{1}{2})=...$	M1
	7.4375 $(7\frac{7}{16})$ $\left(\frac{119}{16}\right)$ (may be implied by correct final answer)	A1
	Uses correct combination of correct areas. Area of region = Area of trapezium − A_1-A_2 **Dependent on all previous method marks**	ddddM1
	$=7.4375-\frac{7}{24}-\frac{4}{3}=\frac{93}{16}$ or 5.8125	A1
		[8]
(c) **Way 2**	**Alternative method using "line – curve"** and subtracting area below x- axis	
	$\int -x^2+\frac{9}{2}x-2\mathrm{d}x=-\frac{x^3}{3}+\frac{9}{4}x^2-2x$ or $\int x^2-\frac{9}{2}x+2\mathrm{d}x=\frac{x^3}{3}-\frac{9}{4}x^2+2x$	M1A1
	Use limits ½ and 4 on this *subtracted* integration $\left(A_3+A_4+A_5+A_6\right)$ = $6\frac{2}{3}+\frac{23}{48}=...$	M1
	$\pm\int x^2-4x+3\mathrm{d}x=\pm\left(\frac{1}{3}x^3-2x^2+3x\right)$	M1
	Use limits 1 and 3 on their integrated curve to obtain A_6 = $\pm\frac{4}{3}$	M1A1
	Uses correct combination of correct areas. Area of region $=\left(A_3+A_4+A_5+A_6\right)-A_6$ **Dependent on all previous method marks**	ddddM1
	$6\frac{2}{3}+\frac{23}{48}-\frac{4}{3}=\frac{93}{16}$	A1
		[8]
(c) **Way 3**	**Alternative method using "line – curve"** for areas A_3 and A_4 and adding smaller trapezium	
	$\int -x^2+\frac{9}{2}x-2\mathrm{d}x=-\frac{x^3}{3}+\frac{9}{4}x^2-2x$ or $\int x^2-\frac{9}{2}x+2\mathrm{d}x=\frac{x^3}{3}-\frac{9}{4}x^2+2x$	M1A1
	Use limits 1 and ½ $[(-\frac{1}{3}(1)^3+\frac{9}{4}(1)^2-2\times 1)-(-\frac{1}{3}(\frac{1}{2})^3+\frac{9}{4}(\frac{1}{2})^2-2\times\frac{1}{2}]$ A_3	M1
	Use limits 4 and 3 $[(-\frac{1}{3}(4)^3+\frac{9}{4}(4)^2-2\times 4)-(-\frac{1}{3}(3)^3+\frac{9}{4}(3)^2-2\times 3]$ A_4	M1
	Area of trapezium = $\frac{1}{2}(a+b)\times h=\frac{1}{2}(\frac{3}{2}+\frac{5}{2})\times(3-1)=...$ or $\int_{1}^{3}(\frac{1}{2}x+1)\mathrm{d}x=\left[\frac{1}{4}x^2+x\right]_{1}^{3}=(\frac{9}{4}+3)-(\frac{1}{4}+1)=...$	M1
	= 4	A1
	Uses correct combination of correct areas. Area of region = $A_3+A_4+A_5$ **Dependent on all previous method marks**	ddddM1
	$\frac{19}{48}+\frac{17}{12}+4=\frac{93}{16}$	A1
		[8]

(c) **Way 4**	**Alternative method: Finds area of larger trapezium and subtracts A$_1$+ A$_2$ which is found by integrating quadratic between ½ and 4 and adding area below *x*-axis**	
	$\int x^2 - 4x + 3 \, dx = \frac{1}{3}x^3 - 2x^2 + 3x$	M1 A1
	Use limits 4 and ½ $[(\frac{1}{3}(4)^3 - 2(4)^2 + 3\times 4) - (\frac{1}{3}(\frac{1}{2})^3 - 2.(\frac{1}{2})^2 + 3\times(\frac{1}{2}))]$ $A_1 + A_2 - A_6$ **AND** Use limits 3 and 1 $\pm[(\frac{1}{3}(3)^3 - 2(3)^2 + 3\times 3) - (\frac{1}{3}(1)^3 - 2.(1)^2 + 3\times(1))]$ $\pm A_6$	M2
	Area of trapezium = $\frac{1}{2}(a+b)\times h = \frac{1}{2}(\frac{5}{4}+3)\times(4-\frac{1}{2}) = ...$ or $\int_{\frac{1}{2}}^{4}(\frac{1}{2}x+1)dx = \left[\frac{1}{4}x^2 + x\right]_{\frac{1}{2}}^{4} = (4+4) - (\frac{1}{16}+\frac{1}{2}) = ...$	M1
	7.4375 $(7\frac{7}{16})$ (may be implied by correct final answer)	A1
	Uses correct combination of correct areas. Area of region $= 7.4375 - (A_1 + A_2 - A_6 + A_6)$ **Dependent on all previous method marks**	ddddM1
	$= 7.4375 - \left(\frac{7}{24} + \frac{4}{3}\right) = \frac{93}{16}$	A1
		[8]
		15 marks
	Notes	
(a)	**M1:** Puts equations equal or finds *x* in terms of *y* and substitutes or substitutes for *x* **dM1:** Solves three term quadratic in *x* to obtain *x* = … or in *y* to obtain *y* = … (Dependent on **first** M) **A1:** Both answers correct **dM1:** Obtains at least one value for *y* or *x* (Dependent on **first** M) **A1:** Both correct **Note:** Allow candidates to obtain $x^2 - \frac{9}{2}x + 2 = 0$ and solve as $(2x-1)(x-4) = 0 \Rightarrow x = \frac{1}{2}, 4$ **The coordinates do not need to be 'paired'**	
(b)	**M1:** Attempts to solve $0 = x^2 - 4x + 3$ according to the usual rules **A1:** cao Attempts by T&I can score both marks for *x* = 1 and *x* = 3. If one solution is obtained by this, score M1A0	
	For (c) do not allow 'mixed' methods. For their strategy, they must be finding the appropriate areas but apply the method for the scheme that gives the most credit for the candidate.	
(c) **Way 1**	**M1:** Attempt at integration of the given quadratic expression $\left(x^n \to x^{n+1} \text{ at least once}\right)$ **A1:** Correct integration of the given quadratic expression **M1:** Finds area of *A*$_1$ **M1:** Finds area of *A*$_2$ **M1:** Finds area of appropriate trapezium **A1:** Correct area of trapezium 7.4375 $(7\frac{7}{16})$ **ddddM1:** correct final combination **A1:** any correct form of this exact answer	
(c) **Way 2**	**M1:** Attempt at integration of ±(the given quadratic expression – the given line) $\left(x^n \to x^{n+1} \text{ at least once}\right)$ **A1:** Correct integration as shown in the mark scheme. Allow correct answer even if terms not collected nor simplified. If there are sign errors when subtracting before valid attempt at integration, score M1A0 **M1:** Uses the limits ½ and 4 on their *subtracted* integration **M1:** Attempts to integrate curve **M1:** Uses the limits 1 and 3 on the integrated curve *C* **A1:** Obtains $A_6 = \pm\frac{4}{3}$ **ddddM1:** correct final combination **A1:** any correct form of this exact answer Note: A common error with this method is to use the limits ½ and 4 on their *subtracted* integration and then stop (this should give an area of $\frac{343}{48}$). This will usually score 3/8 in (c)	

(c) **Way 3**	**M1:** Attempt at integration of ±(the given quadratic expression – the given line) $\left(x^n \to x^{n+1} \text{ at least once}\right)$ **A1:** Correct integration as shown in the mark scheme. Allow correct answer even if terms not collected nor simplified. If there are sign errors when subtracting before valid attempt at integration, score M1A0 **M1:** Uses the limits ½ and 1 on their *subtracted* integration **M1:** Uses the limits 4 and 3 on their *subtracted* integration **M1:** Finds area of appropriate trapezium **A1:** Correct area of trapezium 4 **ddddM1:** correct final combination **A1:** any correct form of this exact answer
(c) **Way 4**	**M1:** Attempt at integration of the given quadratic expression $\left(x^n \to x^{n+1} \text{ at least once}\right)$ **A1:** Correct integration of the given quadratic expression **M2:** Finds area of $A_1 + A_2 - A_6$ by using the limits ½ and 4 **and** finds area of A_6 by using the limits 1 and 3 **M1:** Finds area of appropriate trapezium **A1:** Correct area of trapezium $7.4375\ (7\tfrac{7}{16})$ **ddddM1:** correct final combination **A1:** any correct form of this exact answer

Diagram for Question 16



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